Name:____

CSE341, Winter 2013, Midterm Examination
February 8, 2013

Please do not turn the page until 12:30.

Rules:

- The exam is closed-book, closed-note, except for one side of one 8.5x11in piece of paper.
- **Please stop promptly at 1:20.**
- You can rip apart the pages, but please staple them back together before you leave.
- There are **100 points** total, distributed **unevenly** among **5** questions (all with multiple parts).
- When writing code, style matters, but don't worry much about indentation.

Advice:

- Read questions carefully. Understand a question before you start writing.
- Write down thoughts and intermediate steps so you can get partial credit.
- The questions are not necessarily in order of difficulty. **Skip around.** Make sure you get to all the problems.
- If you have questions, ask.
- Relax. You are here to learn.

Name:_______________________________________

1. This problem uses this datatype binding, where a value of type `points` describes a set of points on the plane, i.e., a 2-D plot with an x-axis and a y-axis.

```
datatype points = Point of real * real
                | Seg of real * real * real * real
                | Union of points * points
                | Shift of points * real * real
```

   - `Point(x,y)` represents the point (x,y).
   - `Seg(x1,y1,x2,y2)` respresents all points on the line segment with endpoints (x1,y1) and (x2,y2).
   - `Union(s1,s2)` represents all points represented by s1 unioned with all points represented by s2.
   - `Shift(s,dx,dy)` represents the points represented by s after shifting them to the right by dx and up by dy.

   Note: we did not use type `real` much in class, but you can use arithmetic operations (e.g., `+`) and comparison operations (e.g., `>`) as expected.

   (a) (**12** points) Write an ML function `rightmost` of type `points -> real * real` such that `rightmost s` returns the point in the set represented by `s` with the largest x-coordinate. (You can resolve ties however you wish.) Notice the result type is `real * real`, the x-coordinate and y-coordinate.

   (b) (**12** points) Write an ML function `max_shifts` of type `points -> int` that given s computes the maximum number of shifts that apply to a single "point" or "segment" in s. Note this is *not* necessarily the number of `Shift` constructors in s. For example, the correct answer for

```
Union(Shift(Point(0.0,0.0),1.0,1.0),
      Shift(Union(Shift(Point(2.0,2.0),1.0,1.0),
                  Shift(Shift(Seg(3.0,4.0,5.0,6.0),7.0,8.0),9.0,10.0)),
             20.0,75.0))
```

   is 3 because the one segment is under three `Shift` constructors, including the one outside the nested `Union`.

Name:____

More room for Problem 1 in case you need it

Name:____

2. This problem uses these two similar but different functions:

```
fun f1 (xs,ys) =
    case (xs,ys) of
        ([], []) => []
      | (x::xs', y::ys') => (x,y)::(f1(xs',ys'))
      | (x::xs', []) => []
      | ([], y::ys') => []

fun f2 (xs,ys) =
    case (xs,ys) of
        ([],[]) => []
      | (x::xs', y::ys') => (x,y)::(f2(xs',ys'))
      | (x::xs', []) => (x,0)::(f2(xs',[]))
      | ([], y::ys') => (0,y)::(f2([],ys'))
```

(a) (**5** points) Fill in the blanks so that `c1` and `d1` are both bound to `[(2,2),(1,1),(0,0)]`

```
val a1 = ____________________

val b1 = ____________________
val c1 = f1(a1,b1)
val d1 = f2(a1,b1)
```

(b) (**5** points) Fill in the blanks so that `d2` but not `c2` is bound to `[(2,2),(1,1),(0,0)]`

```
val a2 = ____________________

val b2 = ____________________
val c2 = f1(a2,b2)
val d2 = f2(a2,b2)
```

(c) (**5** points) Fill in the blanks so that `c3` but not `d3` is bound to `[(2,2),(1,1),(0,0)]`

```
val a3 = ____________________

val b3 = ____________________
val c3 = f1(a3,b3)
val d3 = f2(a3,b3)
```

Name:____

3. For each of the following programs, give the value that `ans` is bound to after evaluation:

   (a) (**4** points)

   ```
   val x = 1
   fun f y =
       let
           val x = y + 1
           val y = x + 1
       in
           y + 1
       end
   val z = f 4
   fun f x = x
   val ans = z
   ```

   (b) (**4** points)

   ```
   val x = 1
   val y = 2
   fun f (g,h) = g x + h y
   val x = 3
   val y = 4
   val ans = f ((fn z => x), (fn z => z))
   ```

   (c) (**4** points)

   ```
   exception E
   val x = 1
   fun f x = if x=2 then raise E else 14
   val x = 2
   val ans = ((f x) + 4) handle E => 9
   ```

   (d) (**4** points)

   ```
   val z = 2
   val f = (fn x => x + 1) o (fn y => if y=z then 4 else y)
   val z = 3
   val ans = List.map f [1,2,3,4,5]
   ```

Name:____

4. (a) (**10** points) Without using any helper functions (such as `foldl`), write an ML function `in_order` that behaves as follows:

   - It takes two arguments *in curried form*: (1) a function `f` that given a list element produces an integer and (2) a list `xs`.
   - It returns true if and only if for all elements of `xs`, `f` applied to the element returns a number less than or equal to `f` applied to any later elements of the list. (This means the result is true for any list with fewer than two elements.)

   (b) (**6** points) Using `in_order`, write a function `shorter_strings` that takes a list of strings and returns true if and only if each string in the list is *longer* than the strings that come later in the list. Hint: You can use ML's ∼ operator for negation.

   (c) (**4** points) What is the type of `in_order`?

   (d) (**2** points) What is the type of `shorter_strings`?

   (e) (**4** points) When your solution to part (a) is given a list `xs` of length n, how many times is the function passed for `f` called before `in_order` returns?

   (f) (**3** points) Suppose another student has a different answer to part (e) and you are both correct because you have different correct answers to part (a). Are your solutions to part (a) *equivalent*? Explain briefly.

Name:____

5. In this problem, suppose we have an ML structure `M` and signature `S` in this standard usage:

```
signature S =
sig
   ...
end
structure M :> S =
struct
   ...
end
```

Assume everything type-checks initially, meaning `M` matches `S`. For each of the following statements, answer "always," "sometimes," or "never."

(**16** points) (2 points each)

(a) If `S` originally contains `val f : int -> int` and we comment out this line, then `M` will still match `S`.

(b) If `S` originally contains `val f : int -> int` and we comment out this line, then a client of `M` will still type-check.

(c) If `S` originally does *not* contain `val g : string -> string` and we add it to `S`, then `M` will still match `S`.

(d) If `S` originally does *not* contain `val g : string -> string` and we add it to `S`, then a client of `M` will still type-check.

(e) If `S` originally contains an abstract type `type t` and we replace this line with `datatype t = Foo of int | Bar of bool`, then `M` will still match `S`.

(f) If `S` originally contains an abstract type `type t` and we replace this line with `datatype t = Foo of int | Bar of bool`, then a client of `M` will still type-check.

(g) If `S` originally contains the line `datatype t = Foo of int | Bar of bool`, and we replace this line with `type t`, then `M` will still match `S`.

(h) If `S` originally contains the line `datatype t = Foo of int | Bar of bool`, and we replace this line with `type t`, then a client of `M` will still type-check.

Name:____

More room in case you need it.